



# **Mathematics**

Advanced GCE Unit **4736:** Decision Mathematics 1

# Mark Scheme for June 2012

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All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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# Mark Scheme

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#### Annotations and abbreviations

Annotation in scoris	Meaning
√and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
Λ	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
M1 dep*	Method mark dependent on a previous mark, indicated by *
сао	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
WWW	Without wrong working

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#### **Subject-specific Marking Instructions**

a Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

c The following types of marks are available.

# Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

#### Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

#### В

Mark for a correct result or statement independent of Method marks.

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Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep \*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.
- g Rules for replaced work

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If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

#### Mark Scheme

h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

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(	Question	Answer	Marks	Guidance	
1	(i)	$\begin{array}{c} A \\ 60 \\ 15 \\ 0 \\ 15 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 13 \\ 0 \\ 10 \\ 1$	M1 A1	Correct graph (exactly this graph, with 10 arcs) (may draw <i>AE</i> so that it does not cross <i>BD</i> ) All arcs correctly weighted Condone weights that are ambiguously placed	
		F	[2]		
1	(ii)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1 A1 B1	Do not allow boxes interchanged condone extra temp labels so we do not need to ft from (i) explicitly <u>Updating</u> from 60 at <i>C</i> (60 as temp and a smaller value as temp or perm) Permanent label 46 at <i>C</i> (seen as perm, not implied) Permanents labels correct at <i>B</i> , <i>D</i> , <i>E</i> and <i>F</i>	
		$\begin{array}{c c} 6 & 49 \\ \hline 49 & F \end{array}$ $A - E - F$	B1 B1 [ <b>5</b> ]	(seen as perm, not implied) (cao) Order of labelling correct at <u>all six</u> vertices, follow through their labels (permanent label, or smallest temporary label if no permanent label shown at a vertex) cao	
1	(iii)	$3 \times \left(\frac{4000}{200}\right)^2 = 3 \times 400 = 1200$	M1	Correct method, including squaring (may be implied from 1200 or from the final answer being 20, www)	$4000 \div 200 = 20$ only $\rightarrow M0$
		or $4000^2 \times 0.000075 = 1200$ or equivalent		May use $\frac{3}{60} = 0.05$ and work in minutes	$\operatorname{Omy} \rightarrow \operatorname{Wid}$
		1200  seconds = 20  minutes	A1 [2]	20 (cao) www	



(	Questio	n	Answer	Marks	Guidance	
2	(ii)	(a)	C1			
			D2 C2	M1	At least six arcs correct, even with extras	
			D1 C3 S2 C4	A1	cao (arcs may be drawn so that they do not cross)	
			S1 M1			
			M2	[2]		
2	(ii)	(h)	C1 C4 M1 M2 and D1 in one session	[2] M1	Two sessions one with C1 and the other with C2	
-	(11)	(0)	C2, C3, S1, S2 and D2 in the other		neither has both C1 and C2	
				A1	cao	
				[2]		
2	(ii)	(c)	M1 and D1 would need to be in different sessions and S2 cannot be in the same session as either of these	M1	A reasonable attempt, involving at least two of D1, M1 and S2 Condone 'M1 and D1 are in the same session' for M1	'M1 and D1 in same session so cannot be done by student at same
				A1	A wholly convincing attempt, <u>explicitly</u> involving all three of D1, M1 and S2 Condone 'D1 M1 and S2 would form a cycle'	time' is not enough for the A mark
				[2]		

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(	Question	Answer	Marks	Guidance		
3	(i)			Check these inputs, tolerance $\pm 0.1$ on y values	For M marks only need	
		$3x + 2y \ge 6$ or $y \ge 3 - 1.5x$ o.e.	M1	$x = 2 \Rightarrow y = 0,  x = 0 \Rightarrow y = 3$	boundary lines correct,	
		$x+y \le 4$ or $y \le 4-x$ o.e.	M1	$x = 3 \Rightarrow y = 1,  x = 1 \Rightarrow y = 3$	$(= < \le > \text{ or } \ge)$	
		$x \le 3y$ and $y \le 2x$	M1	$x = 0 \Rightarrow y = 0,  x = 3 \Rightarrow y = 1$		
		or $y \ge \frac{1}{3}x$ and $y \le 2x$ o.e.		<u>and</u> $x = 0 \Rightarrow y = 0$ , $x = 1 \Rightarrow y = 2$		
			A1	All <u>inequalities</u> correct, and no extras	Only check inequalities if all three M marks achieved	
			[4]			
3	(ii)	$y = \frac{1}{3}x$ meets $y = 4 - x$ at (3, 1)	B1	(3, 1) cao	In (ii), condone ' $x = \dots, y =$	
		$y = 2x$ meets $y = 4 - x$ at $(\frac{4}{3}, \frac{8}{3})$	B1	$(\frac{4}{3},\frac{8}{3})$ o.e. (cao), in fractions	' instead of coordinates	
		$y = \frac{1}{3}x$ meets $y = 3 - 1.5x$ at $(\frac{18}{11}, \frac{6}{11})$	M1	sca <u>using simultaneous equations</u> to find points near both $(1.6, 0.5)$ <u>and</u> $(0.9, 1.7)$ as decimals or fractions ( $\pm$ 0.1 on each coordinate), but not just reading from graph	M1 may be implied from either answer <u>correct</u> as <u>fractions</u> , even if second is wrong or not attempted	
		$y = 2r$ meets $y = 3 = 1.5r$ at $(\frac{6}{12})$	A1	Both $(1\frac{7}{6}, 6)$ o e and $(\frac{6}{12}, 12)$ o e (cao) as frac	rtions	
		$y = 2x \operatorname{meets} y = 5 - 1.5x \operatorname{at} (7, 7)$	[4]	$\underline{\text{Both}}(1_{11}, 1_1) \text{ ote: } \underline{\text{and}}(7, 7) \text{ ote: } (\text{cas}) \text{ as } \underline{\text{max}}$		
3	(iii)	$(3, 1) \rightarrow P - 7$	M1	Calculating $P = r + 4v$ correctly at two of their		
Č	(111)	$(3, 1) \Rightarrow 1 = 7$ $(\frac{4}{2}, \frac{8}{2}) \Rightarrow P = 12$		vertices (vertices may be implied)		
		$ (\frac{18}{11}, \frac{6}{11}) \Rightarrow P = 3\frac{9}{11} (3.82) (\frac{42}{11})  (\frac{6}{7}, \frac{12}{7}) \Rightarrow P = 7\frac{5}{7} (7.71) (\frac{54}{7}) $	A1	All four correct <i>P</i> values shown, as fractions or to $\geq 2$ dp (cao)		
		Optimum point is $(\frac{4}{3}, \frac{8}{3})$ with $P = 12$	B1	$(\frac{4}{3}, \frac{8}{3})$ and 12 (written down) Condone (1.3 to 1.4, 2.6 to 2.7) 11.75 to 12.25	Optimal point in $(x, y)$ form and 12 (within tolerance) written	
2			[3]			
3	(1V)	(2, 2) with $P = 10$	MI	x = 2, $y = 2$ and 10 (written down, whether identified as optimum point and value or not)		
		The only other integer-valued feasible points are $(1, 2), (2, 1)$ and $(3, 1)$ (giving $P = 9, 6$ and 7, respectively, but the <i>P</i> values need not be seen)	A1 [2]	(2, 2) and 10 identified as optimum and a valid explanation that recognises the four integer- valued <u>points</u> that fall in the feasible region	(2, 2) in $(x, y)$ form, could 'identify' using an arrow or star	

Question		Answer	Marks	Guidance	
4	(i)	3x - 4y + z + s = 126x + 2z + t = 20-10x - 5y + 5z + u = 30	B1	Correct use of slack variables ( <i>s</i> , <i>t</i> and <i>u</i> may be in any order) May scale through (e.g. $-2x - y + z + u = 6$ )	Must be + <i>s</i> etc. constraints correct, must have =
		$s \ge 0, t \ge 0, u \ge 0$	B1	s, t and u non-negative (s, t, u 'positive' $\Rightarrow$ B0) Condone $0 \le s \le 12$ etc.	non-negative integers $\Rightarrow$ B0
4	(ii)	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	M1 A1 [2]	Order of rows and columns may be changed $4 \times 8$ table of values (ignore ratio column if shown) <u>and</u> (their) constraint rows correct Objective row correct Assume blanks in initial tableau mean zero	
4	(iii)	(z is the) <u>only</u> column with a negative in objective row $12 \div 1 = 12$ $20 \div 2 = 10$ $30 \div 5 = 6$	B1 B1	x and y have a positive value in the obj row $\Rightarrow$ B1 Need a negative in obj row <u>therefore</u> z column $\Rightarrow$ B1 But 'z most negative in objective row' $\Rightarrow$ B0 'z is negative in objective row' $\Rightarrow$ B0 -5, -6, 4 and (z or 4 is) positive $\Rightarrow$ B0 For the constraint rows, calculate the ratios of the entry in the column for RHS $\div$ entry in (their) pivot column and choose the row with the smallest positive	Need to refer to objective (top) row Do not credit if this appears in part (iv)
		$50 \pm 5 = 0$ 6 is the least positive ratio so pivot on 5 (third constraint, as given in the question)	[2]	ratio (allow sight of 12, 10, 6 and 'smallest' as minimum answer) 12, 10, 6 and an arrow pointing at 6 gets B0	

Question		Answer	Marks	Guidance	
4	(iv)	New pivot row = row $4 \div 5$ New row $1 = row 1 + 4 \times new pivot row$	B1	Correct calculations seen for all four rows, <u>including</u> <u>pivot</u> (accept reasonable abbreviations, eg $\div$ 5, + 4×pr, but not just + 4)	
		New row $2 = row 2 - new pivot row$ New row $3 = row 3 - 2 \times new pivot row$		Pivot row may be shown as individual calculations Some candidates rewrite initial tableau first Some candidates use an interim tableau with new pivot row followed by the full augmented tableau	
		$\begin{array}{c c c c c c c c c c c c c c c c c c c $	M1	A new tableau with 4 basis columns (or 3 with <i>P</i> missing) in which <i>P</i> has not decreased and all entries in RHS column are $\ge 0$	Any column all 0's $\Rightarrow$ M0
		0 -2 -1 1 0 0 0.2 6	A1	cao (rows and columns may be in any order, condone omission of <i>P</i> column) Follow through scaled constraints but not errors from r	part (i)
			[3]	Tonow unough scaled constraints, but not errors, from p	
4	(v)	Pivot on 10 in x column $P$ x       y       z       s       t       u       RHS         1       0       2.6       0       0.3       0.68       26.4         0       0       -4       0       1       -0.5       0       2         0       1       0.2       0       0.1       -0.04       0.8         0       0       -0.6       1       0       0.2       0.12       7.6         x = 0.8, y = 0, z = 7.6 and P = 26.4	M1 A1 B1	A new tableau with 4 basis columns (or 3 with P missing) in which P has not decreased and all entries in RHS column are $\geq 0$ cao (rows and columns may be in any order, condone omission of P column) Follow through scaled constraints, but not errors, from part (i) Strict ft their final tableau for non-negative x, y, z and	Any column all 0's $\Rightarrow$ M0
			[3]	positive P (not P as zero)	
4	(vi)	s = 2, t = 0, u = 0 3x - 4y + z = 10 which is 2 short of 12	B1 B1	Strict ft their final tableau for non-negative <i>s</i> , <i>t</i> , <i>u</i> (all three written down, do not imply blank = 0) Showing what (their) positive value(s) of slack variable(s) mean for the constraint(s)	s, t, u all zero (or any of them negative) $\Rightarrow$ B0 for
		(6x + 2z = 20  and  -10x - 5y + 5z = 30)	[2]		explanation

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Question		Answer	Marks	Guidance	
5	(i)	Odd vertices: M, N, R, W	M1	At least one correct pairing with its weights or total weight (e.g. $MN = 70$ and $RW = 160$ or $MN$ $RW = 100$	
		MN = 70 $MR = 190$ $MW = 90$		230	
		RW = 160 $NW = 150$ $NR = 130$	A1	All three pairings seen with correct total weights (cao)	
		230 340 220		www	
		Total distance = $1200 + 220 = 1420$ metres	B1	1420, condone no units (cao)	
			[3]		
5	(ii)	Just repeat $MN = 70$			
		Total distance = $1200 + 70 = 1270$ metres	M1	1270, condone no units (cao)	
		<i>R</i> and <i>W</i> are still odd so these must be the start and	Al	R and $W$ (from 1270 seen)	
			[2]		
5	(iii)	M-S-W-P-N-V-R-T-M	M1	M-S-W-P-N-V (not a diagram or table)	
-	()	60 + 30 + 170 + 40 + 80 + 50 + 40 + 190	A1	Tour (cycle) listed (cao) with <i>M</i> at each end	
		= 660  metres	B1	660, condone no units (cao)	
				(not 600, which uses $WP = 110$ , from table)	
		Upper bound	B1	$length \le (their) \ 660 \qquad (but < \Rightarrow B0)$	
			[4]		
5	(iv)	$ \begin{array}{c}                                     $	B1	Correct tree Allow SV used instead of NV	Vertices may be shown in different positions to these
		T $V$ $T$ $V$	B1	340 (cao)	
			[2]		
5	(v)	Lower bound = $340 + 30 + 90$	M1	Their 340 + 30 + either 90 or 170	
-				May be implied from 460 as final answer	
		= 460 metres	A1	460, condone no units (cao)	
			[2]		

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Question		n Answer	Marks	Guidance	
6	(i)	A = -4, B = 5, C = 1, X = 0	B1	Initial values for A, B, C and X	
		Y = 1, Z = 5	M1	Y = 1, Z = 5	
		W = -0.2	A1	W = -0.2 (exact, not rounded)	Note: if initial
		X = -0.2			value of $Z = 0$ then
		Y = -0.168, Z = 6.72	M1	Updating Y, Z, W	first value of W
				(showing new values, even if numerically wrong)	occurs when Z first
		W = -0.175	A1	W = -0.175 (-7/40) (exact, not rounded) www	becomes non-zero
					and the next value
		Output -0.2	B1	-0.2 stated (as final X or as output)	is the first update
			[6]		
6	(ii)	A = -4, B = 5, C = 1, X = 1			
		Y = 3, Z = 0	M1	Y = 3, Z = 0	
		X is then reduced to 0 and the algorithm is as	A1	Describing what then happens (' $X = 0$ , then as above',	
		(i) leading to an answer of -0.2		even if part (i) did not lead to -0.2. If values from (i)	
				are written out must get to a second value of <i>W</i> ).	
			[2]		
6	(iii)	A = -4, B = 5, C = 1, X = -1			
		Y = -9, Z = 16	M1	Y = -9, Z = 16	
		W = -0.4375, X = -0.4375	A1	W = -0.4375 (-7/16) (allow -0.437 or -0.438, but not	Note: if initial
				values that round to these)	value of $Z = 0$ see
		Y = -2.04, Z = 9.07	M1	Updating Y, Z and W first time	comment above
		W = -0.213, X = -0.213		(showing new values, even if numerically wrong)	
		Y = -0.256, Z = 6.84	M1	Updating <i>Y</i> , <i>Z</i> and <i>W</i> second time	Dependent on
		W = -0.176	dep	(showing new values, even if numerically wrong)	previous M1
		Root is approximately -0.213	AI	Stopping at -0.213 (or anything that rounds to this)	Dependent on
			r <b>#</b> 3	without wrong working seen	both method marks
	(:)	Marcal	[5]		
0	(1V)	May not converge		Allow could take a long time', 'takes a long time'	
		May not terminate	D1	does not stop, gets stuck in a loop	
		May get stuck in a loop	BI	Any one of these, or similar	
			[1]		

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